

# Candidate Payoffs and Electoral Equilibrium: An Experimental Study

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- We assume that the payoffs of the candidates depend on a number of votes they receive in a general way.
- We find that candidate strategies depend on the vote-payoff relationship.

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- 1970: Won the 1970 Presidential elections on top of a 36.63% plurality (with the runner-up receiving 35.29%)
- 1970-1973: Initiated broad leftist reforms.
- 1973: Lost his life in a coup.

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- Russian anti-corruption activist and opposition leader.
- Is now a candidate in Moscow mayoral election.
- Was convicted in a politically motivated trial and is to serve a 5-year prison sentence.
- Will likely be able to appeal his sentence if his electoral support is high enough.



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# Winning is not all that matters: why a large margin of victory is desirable

Aberto Simpser (2013): In semidemocratic regimes, large victory margins

- Affect the behavior of political elites in the ruler's coalitions.
- Increase the ruler's bargaining powers vis-a-vis business interests and trade unions.
- Deter potential opposition from coordinating.
- Mitigate the pressure to share rents with other groups.

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- 2008 primaries: Mitt Romney is runner-up.
- 2000 primaries: John McCain is runner-up.
- 1988 primaries: Bob Dole is runner-up.
- 1980 primaries: George W. Bush is runner-up.
- 1976 primaries: Ronald Reagan is runner-up.

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# Payoffs are nonlinear in parliamentary systems

- Finally, floor requirement, quotient formula, and district magnitude all affect the translation of votes into seats even in proportional representation electoral systems: Lijphart (1990), Gallagher (1992).
- Coalition-building concerns further complicate the payoff functions of political parties: Snyder, Ting, and Ansolabehere (2005), Laver and Shepsle (1996), Schofield and Sened (2006).

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# The model outline

- Two Downsian candidates and two probabilistic voters.
- Voter 1 is leftist and thinks that Candidate 1 is high quality.
- Voter 2 is rightist and thinks that Candidate 2 is high quality.
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# Theoretic predictions

- If winning by a large margin matters, and losing by a small margin does not, then a candidate will pander to the voters partisan to the opposing candidate.
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## Case study: Navalny's options.

- Low-risk strategy: Campaign on liberal issues. That will secure a small minority of core followers.
- High-risk strategy: Campaign on the more popular issues of immigration and public utilities. That gives a chance of winning over a part of the *a priori* hostile audience. There is also a risk of losing support of the core audience.

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# Candidate objective function equivalence in PVM.

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- 2 Voteshare maximizers vs. probability of win maximizers
- 3 Hinich (1977), Ledyard (1984) — equilibrium equivalence shown for some probability of voter functions
- 4 Patty (2001), Duggan (2000), Patty (2005), Patty (2007) — conditions for both best-response equivalence and equilibrium equivalence are very strict
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## The 2-candidate model: Zakharov (2012)

- There are 2 candidates who compete in an election by choosing policy platforms  $y_1, y_2 \in [0, 1]$ .
- There are two voters, 1 and 2.
- Let  $P_i(y_1, y_2)$  be the probability that voter  $i = 1, 2$  votes for Candidate 1, and  $1 - P_i(y_1, y_2)$  the probability that he votes for Candidate 2.
- Assume that the voters behave according to the utility-difference model:

$$P_i(y_1, y_2) = P(u_{i1} - u_{i2}), \quad (1)$$

where  $u_{ij}$  is the utility that voter  $i$  attributes to Candidate  $j = 1, 2$ , and  $P(\cdot)$  is a continuous, differentiable, strictly increasing function.

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# The 2-candidate model

Let

$$u_{ij} = e_{ij} - \psi(y_j - v_i), \quad (2)$$

where  $e_{ij}$  is the nonpolicy preference of voter  $i$  for Candidate  $j$ ,  $v_i \in [0, 1]$  is the best policy of voter  $i$ , and  $\psi(\cdot)$  is a twice-differentiable disutility function that is symmetric around 0, with  $\psi'(0) = 0$ ,  $\psi'(d) > 0$  for  $d > 0$ , and  $\psi''(d) > 0$ . Let  $v_1 = 0$  and  $v_2 = 1$ .

Without loss of generality, let  $e_{12} = e_{21} = 0$ .

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# Candidate payoffs

There are 3 possible election results:

- 1 Candidate 1 — 0 votes, Candidate 2 — 2 votes
- 2 Candidate 1 — 1 vote, Candidate 2 — 1 vote
- 3 Candidate 1 — 2 votes, Candidate 2 — 0 votes

Let the utility of 0 votes be 0, the utility of 2 votes be 1, and the utility of 1 vote be  $x \in [0, 1]$ .

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## Candidate payoffs

The expected utility functions for both candidates will be

$$U_1 = x((1 - P_1)P_2 + P_1(1 - P_2)) + P_1P_2, \quad (3)$$

$$U_2 = x((1 - P_1)P_2 + P_1(1 - P_2)) + (1 - P_1)(1 - P_2). \quad (4)$$

For  $x = \frac{1}{2}$  the utilities are equal to the expected share of the total vote:  $U_1 = \frac{1}{2}P_1 + \frac{1}{2}P_2$ ,  $U_2 = 1 - \frac{1}{2}P_1 - \frac{1}{2}P_2$ . This special case was analyzed in most of the previous literature.

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# Main result

## Proposition

*Suppose that  $e_{11} = e_{22} = e$ . Let  $P(x) = 1 - P(-x)$ . Then there exists a local equilibrium in the electoral competition game with  $y_1 = 1 - y_2$ .*

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# The comparative statics

## Proposition

Suppose that  $(y, 1 - y)$  is a symmetric equilibrium in the electoral competition game. Then  $y$  decreases with  $x$  for  $x \leq \frac{1}{2}$  and  $y$  increases with  $e$  for  $x < \frac{1}{2}$ . Suppose also that

$$P'(e - \psi(y) + \psi(1 - y))(\psi'(y) + \psi'(1 - y))^3 < \psi'(y)\psi''(1 - y) + \psi'(1 - y)\psi''(y) \quad (5)$$

for all  $y < \frac{1}{2}$ . Then  $y$  decreases with  $x$  for all  $x \in [0, 1]$ . Also,  $y$  increases with  $e$  for  $x < \frac{1}{2}$  and decreases with  $e$  for  $x > \frac{1}{2}$ .



# Comparative statics

In this stylized example, there are 2 voters:

- Voter 1 — partisan of Candidate 1
- Voter 2 — partisan of Candidate 2

If value of getting 1 vote increases, candidates should choose positions closer to those of their partisan voters.

This effect should be stronger if the strength of partisanship —  $e$  — is greater.

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# Comparative statics

## Corollary:

- For  $x = \frac{1}{2}$ ,  $y_1 = y_2$  — mean voter theorem,
- For  $x > \frac{1}{2}$ ,  $y_1 < y_2$ ,
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Suppose that the probability of voting function is logistic:

$$P(u_1 - u_2) = \frac{e^{u_1}}{e^{u_1} + e^{u_2}}, \quad (6)$$

and the disutility functions are taken to be quadratic:

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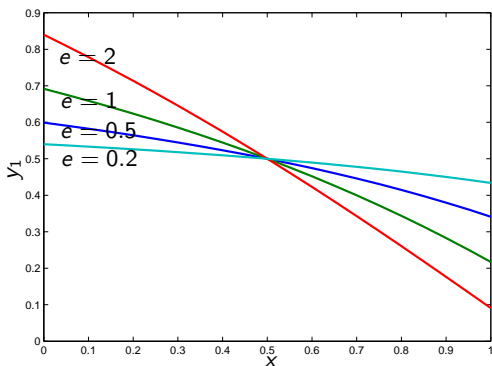
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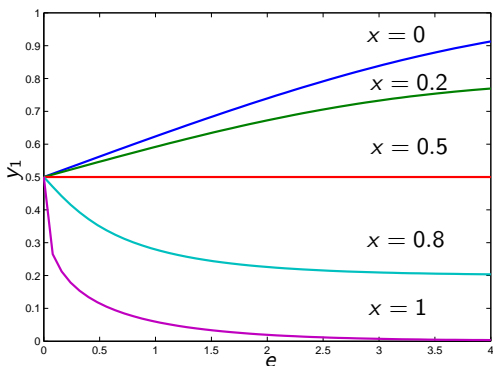
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**Figure :** The equilibrium position of Candidate 1 for different values of  $x$  and  $e$ , with  $\beta = 0.5$

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Let the candidates have the Cobb-Douglas utility function over the number of votes:

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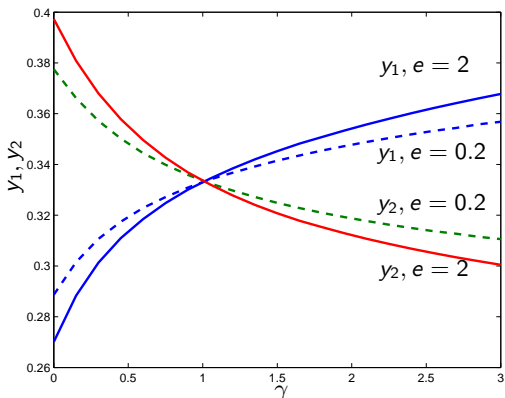
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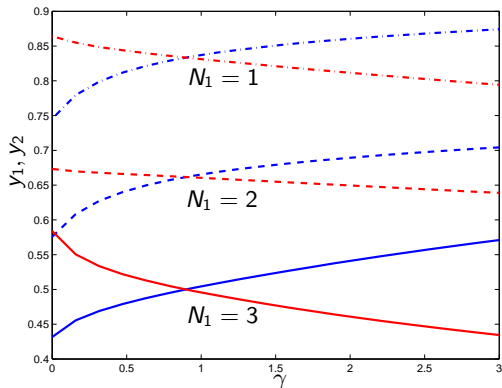
# Comparative statics

Let  $N = 3$  and  $N_1 = 2$ . The candidates had identical utility functions:  $\gamma_1 = \gamma_2 = \gamma$ .





# Comparative statics



As the size of one group increases, the equilibrium is located closer to the other group's voters.

# Design outline

- Experiments were conducted at the FEELE lab at Exeter, using z-Tree.
- We ran 3 treatments. Each treatment had 2 sessions. item Each session had 20 subjects, divided into pairs.
- 120 subjects overall.
- Each pair, played each other for 60 rounds+5 practice rounds.
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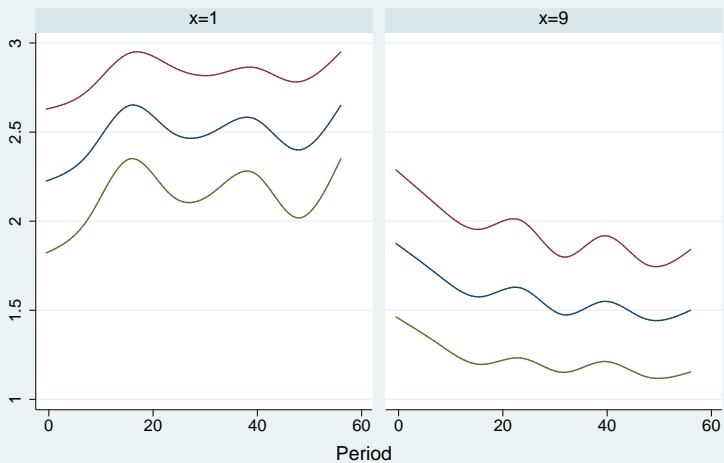
First Event		B's Choice		
		1	2	3
A's Choice	1	94, 6	95, 5	98, 2
	2	93, 7	94, 6	96, 4
	3	50, 50	81, 19	94, 6
Second Event		B's Choice		
		1	2	3
A's Choice	1	6, 94	4, 96	2, 98
	2	19, 81	6, 94	5, 95
	3	50, 50	7, 93	6, 94

# The constant $x$ experiment: Expected payoff matrices.

$x = 1$				
		B's choice		
		1	2	3
A's choice	1	0.21,0.21	0.20,0.20	0.11,0.11
	2	0.22,0.22	0.21,0.21	0.80,0.80
	3	<b>0.30,0.30</b>	0.22,0.22	0.21,0.21
$x = 9$				
		B's choice		
		1	2	3
A's choice	1	0.79,0.79	0.80,0.80	<b>0.88,0.88</b>
	2	0.78,0.78	0.79,0.79	0.80,0.80
	3	0.70,0.70	0.78,0.79	0.79,0.79

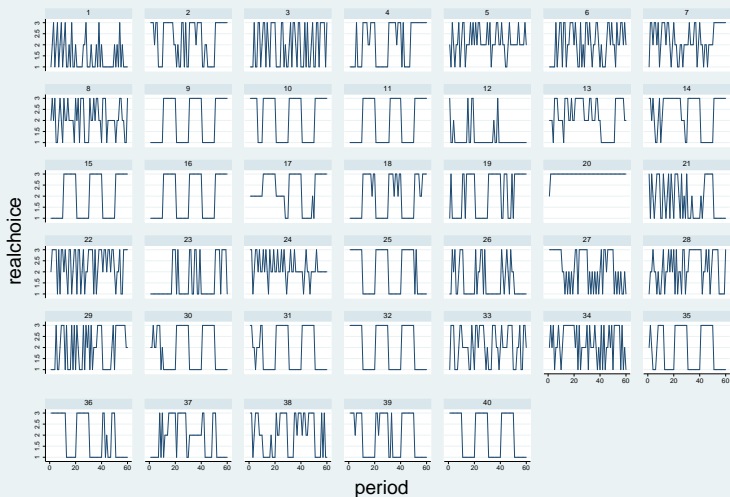
# The constant $x$ experiment

Player choice, mean and 95% confidence interval



Graphs by tr

# The constant $x$ experiment



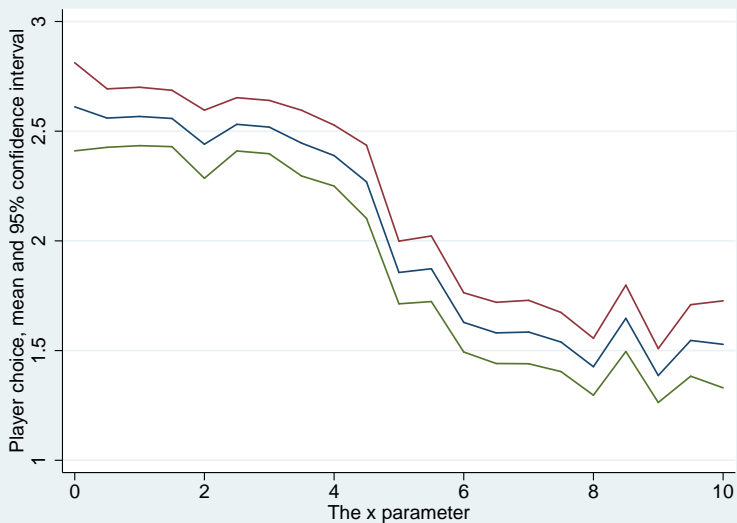
Graphs by subjectnum

# The constant $x$ experiment

Dependent variable is subject's choice (1-3)

Treatment (1 if $x = 1$ )	.76 (0.000)	.801 (0.000)	.95 (0.000)	.85 (0.000)
Period (1-60)	-.0040 (0.002)	-.0034 (0.006)		
Treatment $\times$ Period	.0073 (0.000)	.0061 (0.001)		
Player (1 or 2)	-.098 (0.029)			
Treatment $\times$ Player	-.0266 (0.675)	-.0266 (0.657)		
Opponent's prev. choice				.10 (0.000)
Subject FE	No	Yes	Yes	Yes
Period FE	No	No	Yes	Yes
$N$	2400	2400	2400	2160
Adjusted $R^2$	0.275	0.354	0.354	0.368

# The random $x$ experiment



# The random $x$ experiment: Two equilibria for different $x$

Dependent variable is subject's choice (1-3)

Value of $x$ (0-10)	-0.1119 (0.000)	-0.1061 (0.000)	-0.16 (0.000)
Period (1-60)	.0053 (0.003)	.0056 (0.002)	
$x \times$ Period	-.0011 (0.000)	-.0012 (0.000)	
Player (1 or 2)	-.163 (0.268)	.0304 (0.636)	
$x \times$ Player	-.0073 (0.498)	-.0093 (0.404)	
Subject FE	Yes	No	Yes
Period FE	No	No	Yes
$N$	2400	2400	2400
Adjusted $R^2$	0.3172	0.2526	.0.314

# The random $x$ experiment: Three equilibria for different $x$

Dependent variable is subject's choice (1-3)

Value of $x$ (0-10)	.0338 (0.044)	.0385 (0.033)	-.0019 (0.895)
Period (1-60)	.0035 (0.020)	.0035 (0.033)	
$x \times$ Period	-.0012 (0.000)	-.0012 (0.000)	
Player (1 or 2)	-.441 (0.000)	.4586 (0.000)	
$x \times$ Player	-.093 (0.000)	-.0958 (0.000)	-.0939 (0.000)
Subject FE	Yes	No	Yes
Period FE	No	No	Yes
$N$	2400	2400	2400
Adjusted $R^2$	0.390	0.275	0.388



# The random $x$ experiment: Combined dataset

Dependent variable is subject's choice (1-3)

Value of $x$ (0-10)	-.1069 (0.000)	-.15 (0.000)
Treatment (0 - 2 equilibria)	-.8550 (0.000)	-.21 (0.000)
Treatment $\times x$	.1465 (0.000)	.017 (0.023)
Player (1 or 2)	.0304 (0.615)	
Player $\times x$	-.0093 (0.376)	
Player $\times$ treatment	.4282 (0.000)	
Player $\times$ treatment $\times x$	-.0864 (0.000)	
Period	.0045 (0.000)	
Period $\times x$	-.0012 (0.000)	
Subject FE	No	Yes
Period FE	No	Yes
$N$	4800	4800
Adjusted $R^2$	0.266	0.250

- The experiment confirms the theoretical prediction.
- The predicted effect is stronger later in the experiment.

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Thank you!