# On dual description of the $\operatorname{OSp}(\mathrm{N} \mid 2 \mathrm{~m})$ sigma models <br> Based on M. Alfimov, B. Feigin, B. Hoare and A. Litvinov, to appear 

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## Motivation

- The integrability-preserving deformations of $\mathrm{O}(\mathrm{N})$ sigma models are known to admit the dual description in terms of a coupled theory of bosons and Dirac fermions with exponential interactions of the Toda type (Fateev'04, Litvinov, Spodyneiko'18).
- On the other hand, there are known examples of the integrable superstring theories, such as type IIB $\operatorname{AdS}_{5} \times \mathrm{S}^{5}$ (dual to $\mathcal{N}=4 \mathrm{SYM}$ ) and others, which also have integrable deformations.
- Our strategic goal is to build a similar dual description for the deformed $\mathrm{AdS}_{5} \times \mathrm{S}^{5}$ type IIB superstring and, possibly, other models.
- The building of such a dual description for the superstring theory requires solving three major problems:

1. Incorporate the fermionic degrees of freedom into the construction of dual theory.
2. Adapt the whole construction to describe the sigma models with non-compact target space.
3. The superstring theory possesses the reparametrization symmetry and requires gauge fixing, which makes us include this symmetry into the dual description.

- In the present work we address the first problem generalizing the dual description of the deformed $\mathrm{O}(\mathrm{N})$ sigma models to account for the $\operatorname{OSp}(\mathrm{N} \mid 2 \mathrm{~m})$ sigma models.


## The undeformed $\operatorname{OSp}(\mathrm{N} \mid 2 \mathrm{~m})$ sigma model

- The $\operatorname{OSp}(\mathrm{N} \mid 2 \mathrm{~m})$ sigma model is given by the symmetric space sigma model on the supercoset

$$
\frac{\operatorname{OSp}(N \mid 2 m)}{\operatorname{OSp}(N-1 \mid 2 m)}
$$

- The action for the supergroup-valued field $g \in \operatorname{OSp}(N \mid 2 m)$ is

$$
\mathcal{S}_{0}=-\frac{\mathrm{R}^{2}}{2} \int \mathrm{~d}^{2} \times \mathrm{S} \operatorname{Tr}\left[\mathrm{~J}_{+} \mathrm{PJ} \mathrm{~J}_{-}\right]
$$

where $\mathrm{J}_{ \pm}=\mathrm{g}^{-1} \partial_{ \pm \mathrm{g}} \mathrm{g}$ takes values in the Grassmann envelope of the Lie superalgebra $\mathfrak{o s p}(\mathrm{N} \mid 2 \mathrm{~m} ; \mathbb{R})$ and STr is the invariant bilinear form.

- We are considering the symmetric space with the $\mathbb{Z}_{2}$ grading

$$
\mathfrak{g} \equiv \mathfrak{o s p}(N \mid 2 m ; \mathbb{R})=\mathfrak{g}^{(0)} \oplus \mathfrak{g}^{(1)}, \quad \mathfrak{g}^{(0)}=\mathfrak{o s p}(N-1 \mid 2 \mathfrak{m} ; \mathbb{R})
$$

and P being the projector onto the grade 1 subspace.

- This model is quantum integrable and has the following rational S-matrix (Saleur, Wehefrizt-Kaufmann'01)

$$
\check{S}_{i_{1} i_{2}}^{j_{2} j_{1}}(\theta)=\sigma_{1}(\theta) E_{i_{1} i_{2}}^{j_{2} j_{1}}+\sigma_{2}(\theta) P_{i_{1} i_{2}}^{j_{2} j_{1}}+\sigma_{3}(\theta) I_{i_{1} i_{2}}^{j_{2} j_{1}} .
$$

The coefficients in front of the tensor structures are connected as follows

$$
\sigma_{1}(\theta)=-\frac{2 i \pi}{(N-2 m-2)(i \pi-\theta)} \sigma_{2}(\theta), \quad \sigma_{3}(\theta)=-\frac{2 i \pi}{(N-2 m-2) \theta} \sigma_{2}(\theta)
$$

## Trigonometric $\operatorname{OSp}(\mathrm{N} \mid 2 \mathrm{~m})$ R-matrix and integrable model

- Besides rational solution, the Yang-Baxter equation

$$
\check{R}_{i_{1} i_{2}}^{\mathrm{k}_{2} k_{1}}(\mu) \check{R}_{k_{1} i_{3}}^{k_{3} j_{1}}(\mu+\rho) \check{R}_{k_{2} k_{3}}^{j_{3} j_{2}}(\rho)=\check{R}_{i_{2} i_{3}}^{⿲_{3} k_{2}}(\mu) \check{R}_{i_{1} k_{3}}^{j_{3} k_{1}}(\mu+\rho) \check{R}_{k_{1} k_{2}}^{j_{2} j_{1}}(\rho)
$$

has the trigonometric solution (Bazhanov, Shadrikov'87) with the parameter q.

- Introducing the parametrization

$$
\mathrm{q}=e^{2 \mathrm{i} \pi \lambda}, \quad \mu=(\mathrm{N}-2 \mathrm{~m}-2) \lambda \theta
$$

we observe that for $\lambda=0$ it is consistent with the rational limit and in the special point $\lambda=\frac{1}{2}$ the R -matrix demonstrates an interesting behaviour. It becomes proportional to the S-matrix, corresponding to the scattering of $\frac{N}{2}$ Dirac fermions and $m$ superghost particles in the case of even $N$ and the same plus one boson in the case of odd N .

- Guiding principles to look for the dual description (Litvinov, Spodyneiko'18)

1. The theory with the S-matrix as above has to be renormalizable (at least 1-loop).
2. The dual theory is found as an integrable perturbation from the special point of the S-matrix is determined by the set of screening charges, which commute with the integrals of motion in the leading order in the mass parameter

$$
\left[\mathrm{I}_{\mathrm{k}}^{\mathrm{free}}, \int e^{\left(\boldsymbol{\alpha}_{r}, \phi\right)} d z\right]=0
$$

3. Our model is an integrable deformation of the CFT, based on the coset $\frac{\widehat{0.5 p}(N \mid 2 m) w}{\widehat{0.5 p}(N-1 \mid 2 m) w}$.

## The Yang-Baxter deformation of the $\operatorname{OSp}(\mathrm{N} \mid 2 \mathrm{~m})$ sigma model

- The action for the Yang-Baxter deformed model is (Klimcik'02,Delduc'13)

$$
\mathcal{S}_{\eta}=\int \mathrm{d}^{2} x \mathcal{L}_{\eta}=-\frac{\eta}{2 v} \int \mathrm{~d}^{2} x \mathrm{~S} \operatorname{Tr}\left[\mathrm{~J}_{+} \mathrm{P} \frac{1}{1-\eta \mathcal{R}_{\mathrm{g}} \mathrm{P}} \mathrm{~J}_{-}\right],
$$

where $\eta$ is the deformation parameter and $v$ is the sigma model coupling.

- The operator $\mathcal{R}_{\mathfrak{g}}$ is defined in terms of an operator $\mathcal{R}: \mathfrak{g} \rightarrow \mathfrak{g}$ through

$$
\mathcal{R}_{\mathrm{g}}=\mathrm{Ad}_{\mathrm{g}}^{-1} \mathcal{R} \mathrm{Ad}_{\mathrm{g}},
$$

with $\mathcal{R}$ an antisymmetric solution of the (non-split) modified classical Yang-Baxter equation

$$
\begin{aligned}
& {[\mathcal{R X}, \mathcal{R} Y]-\mathcal{R}([\mathrm{X}, \mathcal{R} \mathrm{Y}]+[\mathcal{R X}, \mathrm{Y}])=[\mathrm{X}, \mathrm{Y}],} \\
& \mathrm{S} \operatorname{Tr}[\mathrm{X}(\mathcal{R} \mathrm{Y})]=-\mathrm{S} \operatorname{Tr}[(\mathcal{R X}) \mathrm{Y}], \quad \mathrm{X}, \mathrm{Y} \in \mathfrak{g} .
\end{aligned}
$$

- In terms of coordinates on the target superspace

$$
\mathcal{L}_{\eta}=\left(\mathrm{G}_{M N}(z)+\mathrm{B}_{M N}(z)\right) \partial_{+} z^{N} \partial_{-} z^{M}, \quad z^{M}=\left(x^{\mu}, \psi^{\alpha}\right),
$$

where $G_{M N}=(-1)^{M N} G_{N M}$ and $B_{M N}=-(-1)^{M N} B_{N M}$.

- We explicitly calculated $\mathrm{G}_{\mathrm{MN}}(z)$ and $\mathrm{B}_{\mathrm{MN}}(z)$ in the range of parameters $\mathrm{N}=1, \ldots, 8$ and $\mathrm{m}=1,2,3$.


## Ricci flow

- Substituting the metric and Kalb-Ramond field of the deformed $\operatorname{OSp}(\mathrm{N} \mid 2 \mathrm{~m})$ sigma model for $\mathrm{m}=1$ with $\mathrm{N}=1, \ldots, 6$ into the Ricci flow equation

$$
R_{M N}+\frac{d}{d t} E_{M N}+\left(\mathcal{L}_{Z} E\right)_{M N}+(d Y)_{M N}=0, \quad E_{M N}=G_{M N}+B_{M N}
$$

we indeed find $\left(t \sim \log \Lambda_{u v}\right)$

$$
\frac{d v}{d t}=0, \quad \frac{d \eta}{d t}=-v(N-2 m-2)\left(1+\eta^{2}\right)
$$

which is the natural expectation for general N and m . It agrees with the known result for $\mathrm{m}=0$ (Squellari'14, Litvinov, Spodyneiko'18).

- Taking $v=\eta R^{-2}$ with $\eta \rightarrow 0$, we find the RG flow in the undeformed limit

$$
\frac{d R^{2}}{d t}=-(N-2 m-2)
$$

- Solving the renormalisation group flow equations for real $\eta$ we find cyclic solutions. This motivates us to consider the analytically-continued regime

$$
v \rightarrow i v, \quad \eta \rightarrow i k
$$

in which we have ancient solutions. In this regime the solution is

$$
v=\text { constant }, \quad k=-\tanh (v(N-2 m-2) t) .
$$

- Therefore the model in question is asymptotically free in the UV for $\mathrm{N}-2 \mathrm{~m}>2$. From now on we will concentrate on the simplest case of this type, i.e. $N=5$ and $m=1$ or $\operatorname{OSp}(5 \mid 2)$.


## $\operatorname{OSp}(\mathrm{N} \mid 2 \mathrm{~m})$ action from $\mathrm{O}(\mathrm{N}+2 \mathrm{~m})$ action

- Although the general form of this trick is known to us, for conciseness let us consider the case $N=2 n+1$ and $m=1$. The simplest way to write the deformed $\mathrm{O}(2 n+1) / \mathrm{O}(2 n)$ action is to use "stereographic" coordinates

$$
\mathrm{ds} s^{2}=\sum_{\mathrm{k}=1}^{n} \frac{\kappa_{k}}{v} \frac{\mathrm{~d} z_{\mathrm{k}} \mathrm{~d} \bar{z}_{\mathrm{k}}}{\left(1+z_{\mathrm{k}} \bar{z}_{k}\right)^{2}\left(1-\kappa_{k}^{2}\left(\frac{1-z_{k} \bar{z}_{k}}{1+z_{k} \bar{z}_{k}}\right)^{2}\right)},
$$

where

$$
\kappa_{k}=\kappa \prod_{j=1}^{k-1}\left(\frac{1-z_{j} \bar{z}_{j}}{1+z_{j} \bar{z}_{j}}\right)^{2}, \quad k=1, \ldots, n
$$

- The transition to different deformations $\operatorname{OSp}(\mathrm{N} \mid 2)$ action from the $\mathrm{O}(\mathrm{N}+2)$ is made by the substitution for some $z_{k}$

$$
z_{\mathrm{k}} \rightarrow \frac{\psi}{\sqrt{2}}=\frac{\psi^{1}+i \psi^{2}}{\sqrt{2}}, \quad \bar{z}_{\mathrm{k}} \rightarrow \frac{\bar{\psi}}{\sqrt{2}}=\frac{\psi^{1}-i \psi^{2}}{\sqrt{2}} .
$$

Further we concentrate on the case $k=1$.

- Also we go back to the "spherical" parametrization of the coordinates $z_{j}$

$$
z_{j}=\sqrt{2 \frac{1-r_{j}}{1+r_{j}}} e^{i \phi_{j}}
$$

## The deformed $\operatorname{OSp}(5 \mid 2)$ sigma model action

- Let us now turn to the specific case $\operatorname{OSp}(5 \mid 2)$. The deformed sigma model is parametrised by four bosons, $\phi_{1}, \phi_{2}, r_{1}$ and $r_{2}$, and a symplectic fermion, $\psi^{a}$, where $a=1,2$.
- The Lagrangian following from the previous slide is

$$
\left.\begin{array}{l}
\mathcal{L}_{\kappa}=\frac{\kappa\left(1-\kappa^{2} r_{1}^{2}+\left(1+\kappa^{2} r_{1}^{2}\right) \psi \cdot \psi\right)}{v\left(1-\kappa^{2} r_{1}^{2}\right)^{2}}\left[\frac{\partial_{+} r_{1} \partial_{-} r_{1}}{1-r_{1}^{2}}+\left(1-r_{1}^{2}\right) \partial_{+} \phi_{1} \partial_{-} \phi_{1}\right. \\
\left.+i \kappa r_{1}(1+\psi \cdot \psi)\left(\partial_{+} r_{1} \partial_{-} \phi_{1}-\partial_{+} \phi_{1} \partial_{-} r_{1}\right)\right] \\
+\frac{\kappa r_{1}^{2}\left(1-\kappa^{2} r_{1}^{4} r_{2}^{2}+\left(1+\kappa^{2} r_{1}^{4} r_{2}^{2}\right) \psi \cdot \psi\right)}{v\left(1-\kappa^{2} r_{1}^{4} r_{2}^{2}\right)^{2}}\left[\frac{\partial_{+} r_{2} \partial_{-} r_{2}}{1-r_{2}^{2}}+\left(1-r_{2}^{2}\right) \partial_{+} \phi_{2} \partial_{-} \phi_{2}\right. \\
\left.+i \kappa r_{1}^{2} r_{2}(1+\psi \cdot \psi)\left(\partial_{+} r_{2} \partial_{-} \phi_{2}-\partial_{+} \phi_{2} \partial_{-} r_{2}\right)\right]
\end{array} \quad \begin{array}{l}
\kappa\left(1-\kappa^{2}+\frac{1}{2}\left(1+\kappa^{2}\right) \psi \cdot \psi\right) \\
v\left(1-\kappa^{2}\right)^{2}
\end{array} \partial_{+} \psi \cdot \partial_{-} \psi-i \kappa\left(1+\frac{1}{2} \psi \cdot \psi\right) \partial_{+} \psi \wedge \partial_{-} \psi\right], ~ \$
$$

where we have introduced the following contractions of the symplectic fermion

$$
x \cdot x^{\prime}=\epsilon_{a b} x^{a} x^{\prime b}, \quad x \wedge x^{\prime}=\delta_{a b} x^{a} x^{\prime b}
$$

## UV limit of the deformed $\operatorname{OSp}(5 \mid 2)$ sigma model

- We are interested in the expansion around the UV fixed point, that is $k=1$. The specific limit we consider (Litvinov'18) is given by first setting

$$
r_{1}=\exp \left(-\epsilon e^{-2 x_{1}}\right), \quad r_{2}=\tanh x_{2}, \quad \psi^{a}=\epsilon \theta^{a}, \quad \kappa=1-\frac{\epsilon^{2}}{2},
$$

and subsequently expanding around $\epsilon=0$.

- Introducing the complex fields

$$
X_{1}=x_{1}-\mathfrak{i} \phi_{1}, \quad X_{2}=x_{2}-\mathfrak{i} \phi_{2}, \quad \Theta=\theta^{1}-\mathfrak{i} \theta^{2},
$$

we find the following expansion

$$
\begin{aligned}
\mathcal{L}_{k \sim 1}=\frac{1}{v}\left(\partial_{+}\right. & \left.X_{1} \partial_{-} X_{1}^{*}+\partial_{+} X_{2} \partial_{-} X_{2}^{*}+i\left(1-i \Theta \Theta^{*}\right) \partial_{+} \Theta \partial_{-} \Theta^{*}\right) \\
& \quad-\frac{\epsilon}{v}\left(\frac{1}{2} e^{2 x_{1}}\left(1+2 i \Theta \Theta^{*}\right) \partial_{+} X_{1} \partial_{-} X_{1}^{*}+\right. \\
+ & \left.e^{-2 x_{1}+2 x_{2}} \partial_{+} X_{2} \partial_{-} X_{2}^{*}+e^{-2 x_{1}-2 x_{2}} \partial_{+} X_{2}^{*} \partial_{-} X_{2}\right)+\mathcal{O}\left(\epsilon^{2}\right),
\end{aligned}
$$

up to total derivatives.

## Screening charges for the deformed $\operatorname{OSp}(5 \mid 2)$ sigma model

- We propose dual description of $\operatorname{OSP}(5 \mid 2)$ deformed sigma-model. Its system of screening charges is the following

- The vectors $\alpha_{r}$ can be parameterized as follows ( $\beta=\sqrt{1+b^{2}}$ )

$$
\begin{array}{lll}
\alpha_{1}=b E_{1}+i \beta e_{1}, & \alpha_{2}=-b E_{1}+i \beta e_{1}, & \alpha_{3}=-b E_{2}-i \beta e_{1}, \\
\alpha_{4}=b E_{2}+i \beta e_{2}, & \alpha_{5}=\frac{i}{\beta} e_{2}+\frac{i b}{\beta} e_{3}, & \alpha_{6}=-\frac{2 i b}{\beta} e_{3},
\end{array}
$$

- To restore the sigma model metric in the UV limit, we have to use the fact (Litvinov, Spodyneiko'16) that for the pair of the neighbouring fermionic exponential screenings $e^{\left(\alpha_{1}, \phi\right)}$ and $e^{\left(\alpha_{2}, \phi\right)}$ the dressed screenings

$$
\left(\boldsymbol{\alpha}_{1,2}, \phi\right) e^{\left(\boldsymbol{\beta}_{12}, \phi\right)}, \quad \boldsymbol{\beta}_{12}=\frac{2\left(\boldsymbol{\alpha}_{1}+\boldsymbol{\alpha}_{2}\right)}{\left(\boldsymbol{\alpha}_{1}+\boldsymbol{\alpha}_{2}\right)^{2}}
$$

commute with the same system of the integrals of motion.

## Metric for the deformed $\operatorname{OSp}(5 \mid 2)$ sigma model

- By taking the dual screenings we obtain the following system, which includes the dressed screenings

- By choosing $z=x^{1}-i x^{2}\left(\bar{z}=x^{1}+i x^{2}\right)$ and then conducting Wick rotation $\chi^{2}=i \chi^{0}$, we obtain the action in Minkowski signature

$$
\begin{aligned}
& \mathcal{L}=\frac{1}{2 \pi}\left(\sum_{i=1}^{2}\left(\partial_{+} \Phi_{i}\right)\left(\partial_{-} \Phi_{i}\right)+\sum_{j=1}^{3}\left(\partial_{+} \phi_{j}\right)\left(\partial_{-} \phi_{j}\right)\right)+ \\
& + \\
& +\Lambda_{1}\left(\partial_{+}\left(b \Phi_{1}+i \beta \phi_{1}\right) \partial_{-}\left(b \Phi_{1}-i \beta \phi_{1}\right) e^{\frac{\Phi_{1}-\Phi_{2}}{b}}+\right. \\
& \left.+\partial_{+}\left(b \Phi_{1}-i \beta \phi_{1}\right) \partial_{-}\left(b \Phi_{1}+i \beta \phi_{1}\right) e^{-\frac{\Phi_{2}+\Phi_{1}}{b}}\right)+ \\
& +\Lambda_{2} \partial_{+}\left(b \Phi_{2}+i \beta \phi_{2}\right) \partial_{-}\left(b \Phi_{2}-i \beta \phi_{2}\right) e^{\frac{\Phi_{2}}{b}-\frac{i \beta}{b} \phi_{3}+\Lambda_{3} e^{\frac{i \beta}{b} \phi_{3}}+(\text { counterterms })+\ldots,}
\end{aligned}
$$

## Restoring the deformed $\operatorname{OSp}(5 \mid 2)$ sigma model in the UV limit

- Then we fermionize the $\phi_{3}$ field and add the counterterms appearing because of the corrections, coming from the fermionic loops. This after the integrations over the $\Psi_{1}$ and $\Psi_{2}^{\dagger}$ components yields the following action

$$
\begin{aligned}
& \mathcal{L}=\frac{1}{2 \pi}\left(\sum_{i=1}^{2}\left(\partial_{+}+\Phi_{i}\right)\left(\partial_{-} \Phi_{i}\right)+\sum_{j=1}^{2}\left(\partial_{+} \phi_{j}\right)\left(\partial_{-} \phi_{j}\right)\right)+ \\
& \\
& +\Lambda_{1}\left(\partial_{+}\left(b \Phi_{1}+i \beta \phi_{1}\right) \partial_{-}\left(b \Phi_{1}-i \beta \phi_{1}\right) e^{\frac{\Phi_{1}-\Phi_{2}}{b}}+\right. \\
& \\
& +\partial_{+}\left(b \Phi_{1}-i \beta \phi_{1}\right) \partial_{-}\left(b \Phi_{1}+i \beta \Phi_{1}\right) e^{\left.-\frac{\Phi_{2}+\Phi_{1}}{b}\right)-} \\
& \\
& \quad-i \Lambda_{2} \partial_{+}\left(b \Phi_{2}+i \beta \phi_{2}\right) \partial_{-}\left(b \Phi_{2}-i \beta \phi_{2}\right) \psi_{1}^{\dagger} \psi_{2} e^{\frac{\Phi_{2}}{b}+} \\
& +\frac{4 i}{\Lambda_{3}} \partial_{+} \psi_{2} \partial-\psi_{1}^{\dagger}+\frac{8 \pi}{\beta^{2} \Lambda_{3}^{2}} \psi_{1}^{\dagger} \psi_{2} \partial_{+} \psi_{2} \partial-\psi_{1}^{\dagger}+\Lambda_{2} \partial_{+}\left(b \Phi_{2}+i \beta \phi_{2}\right) \partial-\left(b \Phi_{2}-i \beta \phi_{2}\right) e^{\frac{\Phi_{2}}{b}+\ldots,}
\end{aligned}
$$

- Upon identifying $\Phi_{1,2}=2 \mathrm{bx}_{2,1}, \phi_{1,2}=2 \mathrm{~b} \varphi_{2,1}$ and $\Psi_{1}^{\dagger}=\mathrm{b} \Theta^{*}, \Psi_{2}=\mathrm{b} \Theta$ together with taking the limit $\mathrm{b} \rightarrow \infty$ and adjusting properly the coefficients $\Lambda_{1,2,3}\left(\alpha^{\prime}=\frac{2}{\mathrm{~b}^{2}}\right)$ we obtain

$$
\begin{gathered}
\mathcal{L}=\frac{1}{4 \pi \alpha^{\prime}}\left(\left(\sum_{i=1}^{2}\left(\partial_{+} x_{i}\right)\left(\partial_{-} x_{i}\right)+\sum_{j=1}^{2}\left(\partial_{+} \varphi_{j}\right)\left(\partial_{-} \varphi_{j}\right)+i\left(1-i \Theta \Theta^{*}\right) \partial_{+} \Theta \partial_{-} \Theta^{*}\right)-\right. \\
-\Lambda\left(\partial_{+}\left(x_{2}+i \varphi_{2}\right) \partial_{-}\left(x_{2}-i \varphi_{2}\right) e^{2 x_{2}-2 x_{1}}+\partial_{+}\left(x_{2}-i \varphi_{2}\right) \partial_{-}\left(x_{2}+i \varphi_{2}\right) e^{-2 x_{2}-2 x_{1}}+\right. \\
\left.\left.+\partial_{+}\left(x_{1}+i \varphi_{1}\right) \partial_{-}\left(x_{1}-i \varphi_{1}\right)\left(\frac{1}{2}+i \Theta \Theta^{*}\right) e^{2 x_{1}}\right)+\ldots\right)+\mathcal{O}\left(\alpha^{\prime 0}\right)
\end{gathered}
$$

## Conclusions and outlook

- We found the action of the $\eta$-deformed $\operatorname{OSp}(\mathrm{N} \mid 2 \mathrm{~m})$ sigma models for several N and m and put forward the hypothesis how to generate this action for general N and m .
- The 1-loop RG flow of such models was studied and we found the UV stable solutions. We considered the scaling limit of the deformed $\operatorname{OSp}(5 \mid 2)$ sigma model action as an example.
- The system of screening charges, which determine the integrable structure of the $\operatorname{OSp}(\mathrm{N} \mid 2)$ sigma model was built.
- By using it we demonstrated how to restore the sigma model action in the deep UV in the case of $\operatorname{OSp}(5 \mid 2)$.
- Utilizing our system of screenings to write the dual model with the Toda type interactions we can reproduce the expansion of the $S$-matrix in the vicinity of the special point $\lambda=\frac{1}{2}$ (work in progress).
- The next interesting step would be to try to adapt the dual description for the sigma models with the non-compact target space (Basso, Zhong'18).

Thanks for your attention!

